Condor: Supercomputing Without a Super-Budget

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Outline

- Introduction to Condor
 - Why Condor
 - Condor Overview
 - Running your first Condor job
 - Managing Condor jobs
- 2 Condor Recipes
 - Automatic checkpoint of long-running codes
 - Statistical Bootstrapping
 - DAGMAN: Coordinating dependent jobs
 - Condor and GAMS
- 3 Master-Worker: Parallel Programming Using Condor
 - Master-Worker
 - An MW Example: Value Function Iteration
 - The World of Condor

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Introduction to Condor

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Introduction to Condor

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- Amazon.com EC2: 10 cents/hour
- Academic computing: 4 cents/hour
- Opportunistic computing: even cheaper

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Why Condor Condor Overview Running your first Condor job Managing Condor jobs

Condor is a cluster computing manager for HTC HTC: High Throughput Computing

- High Throughput Computing, not
- High Performance Computing
- Dedicated Clusters
- Cycle scavanging from desktops
- Clusters of Clusters (The Grid)

Summary

Why Condor Condor Overview Running your first Condor job Managing Condor jobs

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HTC and the grid



Maximum: 3,242,512 Hours, Minimum: 155,142 Hours, Average: 2,336,628 Hours, Current: 2,109,872 Hours

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Installing Condor

• Call your IT department!

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Typical Condor pool



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Three steps to cluster computing

- Prepare your job and inputs
- Write a submit_file
- Run and manage your job

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Step 1: Prepare your job

- Like going on vacation pack carefully!
- Check for library and other dependencies
- Run condor_compile for checkpointed
- Gather all inputs together

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Step 2: Write a submit file Submit file describes your jobs to Condor

submit_file

universe = vanilla

```
executable = /usr/bin/matlab
arguments = gonkulate.m
```

```
transfer_input_files = gonkulate.m
should_transfer_files = yes
when_to_transfer_output = always
```

```
output = out
error = err
log = log
queue 1
```

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Step 3: Submit your job(s)

Shell prompt

condor_submit submit_file
Submitting job(s)....
Logging submit event(s)....
1 job(s) submitted to cluster 11.

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Step 3a: Manage your job(s)

Shell prompt

condor_rm my_job_number condor_hold my_job_number condor_release my_job_number

condor_q condor_q -run

condor_status

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Long running jobs

What if you need to run a job that takes a month to run?

- And the machine crashes?
- Or loses power?
- Or gets rebooted?

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Long running jobs

Solution: Checkpointing!

- Condor can periodically save the whole state of the job
- And restore it on a another machine, if needed

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Running Standard Universe Jobs

- condor_compile your code
 - condor_compile gcc -o solver solver.c
 - condor_compile f77 -o executable source.f
- indicate Standard universe in your submit file
- Submit as normal
- If execute machine dies, Condor restarts the job elsewhere
- If submit machine dies, Condor restarts the job elsewhere

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Example: Statistical Bootstrapping

A Parameter Sweep



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Example: Statistical Bootstrapping

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Example: Statistical Bootstrapping

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Example: Statistical Bootstrapping

A Parameter Sweep



Example: Statistical Bootstrapping

A Parameter Sweep



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Statistical Bootstrapping A Condor/Matlab implementation

Driver Creates distribution.

Driver Creates submit file.

Driver Runs

condor_submit.

Norkers Analyzes subset

Driver Processes results.

driver.m

dist_size = 100000; d = rand(dist_size, 1) .* 500; subset = d(floor(rand(1000,1) .* 100000)); save "subset" subset;

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Statistical Bootstrapping A Condor/Matlab implementation

Driver Creates distribution.

Driver Creates submit file.

Driver Runs condor_submit.

Norkers Analyzes subset

Driver Processes results.

Generated submit_file

universe = vanilla executable = worker.m transfer_files = true when_to_transfer_output = on_exit transfer_input_files = subset output = mean.\$(PROCESS) log = log queue 5

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Statistical Bootstrapping A Condor/Matlab implementation

Driver Creates distribution.

Driver Creates submit file.

Driver Runs

condor_submit.

Norkers Analyzes subset

Driver Processes results.

driver.m

system("condor_submit file");
system("condor_wait log");

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Automatic checkpoint of long-running codes Statistical Bootstrapping DAGMAN: Coordinating dependent jobs Condor and GAMS

Statistical Bootstrapping A Condor/Matlab implementation

Driver Creates distribution.

Driver Creates submit file.

Driver Runs

condor_submit

Norkers Analyzes subset

Driver Processes results.

worker.m – All in parallel

load "subset" subset; subset = subset(floor(rand(10,1) .* 1000)); printf("%f ", mean(subset));

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Statistical Bootstrapping A Condor/Matlab implementation

Driver Creates distribution. Driver Creates submit file. Driver Runs condor_submit. Jorkers Analyzes subset

Driver Processes results.

driver.m

while (jobs- > 0)
tmp = sprintf("mean.%d", jobs);
f = fopen(tmp, "rb", "native");
val = fscanf(f, "%f");
results(jobs + 1) = val;
endwhile
result = mean(results);

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Running the example

Shell prompt

\$./driver.m
Submitting job(s)....
Logging submit event(s)....
5 job(s) submitted to cluster 565262.

5 minutes later...

All jobs done. mean of mean is 161.014978 Introduction to Condor Condor Recipes Master-Worker: Parallel Programming Using Condor Summary Automatic checkpoint of long-running codes Statistical Bootstrapping DAGMAN: Coordinating dependent jobs Condor and GAMS

DAGMan DAGMan: Directed Acyclic Graph Manager

- Often there are dependencies between the individual jobs that make up your application.
- One job's output is another's input.
- The relationships between the different jobs are known a priori, and not generated dynamically during execution.
- Possibly there are many such relationships in your application.

DAGMan is intended for applications like this.

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DAGMan Example problem

Example

- 2-D Matrix of Condor jobs
- Each job has two inputs
 - From leftmost neighbor
 - From lower neighbor
- Initial conditions known
- Desire maximum concurrency



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DAGMan Example problem

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DAGMan Example problem

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DAGMAN description file

- JOB section names each node and its submit file
- PARENT section describes dependencies
- VARS section names variable to expand in submit file

DAG file

```
JOB Node_1_1 node.sub
JOB Node_2_1 node.sub
JOB Node_2_2 node.sub
```

```
PARENT Node_1_2 Node_2_1 CHILD Node_2_2
```

```
...
VARS Node_2_2 in1="f12"
VARS Node_2_2 in1="f21"
VARS Node_2_2 out="f22" ...
```

submit

```
universe = vanilla
```

```
executable = sum.pl
arguments = $(IN1) $(IN2) $(IN3)
```

```
should_transfer_files = yes
when_to_transfer_output = on_exit
```

```
transfer_input_files = $(IN1), $(IN2), $(IN3)
```

output = \$(OUT) log = log

```
Notification = never queue
```

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Running dagman

submit

\$ condor_dag_submit grid.dag

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Condor and GAMS Using the Grid support within GAMS

- A new feature of GAMS!
- GAMS itself writes submit files, calls condor_submit
- Uses Condor script to glue the pieces together

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Condor and GAMS

New GAMS Commands

```
<model>.solvelink = 3
```

;do not wait for solve, just submit

<model>.handle (set by the 'submitting' solver)

HandleStatus(handle) =

- 0 bad handle
- 1 model ready to solve but no solution
- 2 solution ready to be extracted

executeloadhandle model

; loads all equ and var info

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Condor and GAMS Running it

Shell Prompt

gamskeep transgrid10.gms

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Master-Worker An MW Example: Value Function Iteration

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Master-Worker An MW Example: Value Function Iteration

Two Condor Shortcomings

- Condor doesn't run short jobs well.
 - lots of time required to schedule jobs in the pool;
 - time needed to transmit the executable/data/results.
- Condor doesn't deal directly with parallel algorithms.
 - Can have the process on the user's workstation generating waves of "worker" jobs to run in parallel, but
 - each worker job must be scheduled anew in the Condor pool, and
 - the master application has to handle all the details of scheduling, rescheduling after faults, managing input and outputs to workers, etc.

Master-Worker (MW) addresses these issues!

Master-Worker An MW Example: Value Function Iteration

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Master-Worker: Basic Ideas

- Master assigns tasks to the workers
- Workers perform tasks, and report results back to master
- Workers do not communicate (except through the master)
- Simple!
- Fault-tolerant
- Oynamic
- Programming model reusable across many applications.

Master-Worker An MW Example: Value Function Iteration

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Other Important Features!

- Data common to all tasks is sent to workers only once
- (Try to) Retain workers until the whole computation is complete—don't release them after a single task is done.

These features make for much higher parallel efficiency.

- We now need to transmit much less data between master and workers.
- We avoid the overhead of putting each task on the condor queue and waiting for it to be allocated to a processor.

Master-Worker An MW Example: Value Function Iteration

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MW

- Three abstractions in the master-worker paradigm: Master, Worker, and Task.
- The MW package encapsulates these abstractions
 - C++ abstract classes
 - User writes 10 functions (Templates and skeletons supplied in distribution)
 - The MWized code will adapt transparently to the dynamic and heterogeneous environment
- The back side of MW interfaces to resource management and communications packages:
 - Condor/PVM, Condor/Files
 - Condor/Unix Sockets
 - Single processor (useful for debugging)
 - In principle, could use other platforms.

Master-Worker An MW Example: Value Function Iteration

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MW Classes

MWMaster

- get_userinfo()
- setup_initial_tasks()
- pack_worker_init_data()
- act_on_completed_task()
- MWTask
 - (un)pack_work
 - (un)pack_result
- MWWorker
 - unpack_worker_init_data()
 - execute_task()

Master-Worker An MW Example: Value Function Iteration

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But wait there's more!

- User-defined checkpointing of master. (Don't lose the whole run if the master crashes.)
- (Rudimentary) Task Scheduling
 - MW assigns first task to first idle worker
 - Lists of tasks and workers can be arbitrarily ordered and reordered
 - User can set task rescheduling policies
- User-defined benchmarking
 - A (user-defined) task is sent to each worker upon initialization
 - By accumulating normalized task CPU time, MW computes a performance statistic that is comparable between runs, though the properties of the pool may differ between runs.

Master-Worker An MW Example: Value Function Iteration

MW Applications

- MWFATCOP (Chen, Ferris, Linderoth) A branch and cut code for linear integer programming
- MWQAP (Anstreicher, Brixius, Goux, Linderoth) A branch-and-bound code for solving the quadratic assignment problem
- MWATR (Linderoth, Shapiro, Wright) A trust-region-enhanced cutting plane code for two-stage linear stochastic programming and statistical verification of solution quality.
- MWKNAP (Glankwamdee, Linderoth) A simple branch-and-bound knapsack solver
- MWAND (Linderoth, Shen) A nested decomposition-based solver for multistage stochastic linear programming
- MWSYMCOP (Linderoth, Margot, Thain) An LP-based branch-and-bound solver for symmetric integer programs

Master-Worker An MW Example: Value Function Iteration

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Wealth Accumulation

Given initial capital stock x_0 , find $V(x_0)$

$$V(x_0) = \begin{cases} \max_{\substack{(c_t, l_t) \\ s.t. \end{cases}}} \sum_{t=0}^{\infty} \beta^t u(c_t, l_t) \\ s.t. \quad x_{t+1} = x_t + f(x_t, l_t) - c_t \end{cases}$$

- ct and lt are consumption and labor supply at time t
- capital evolves according to $x_{t+1} = x_t + f(x_t, l_t) c_t$
- β is the discount factor and $u(c_t, l_t)$ is the utility given consumption c_t and labor supply l_t
- V(x) is the value function for $x_0 = x$

Master-Worker An MW Example: Value Function Iteration

Dynamic Programming

An optimization problem with infinitely many variables: c_t , l_t , x_t , t = 0, 1, 2, ..., so it's hard to attack it directly.

But we can use the *dynamic programming principle*, because the optimal objective $V(x_0)$ depends only on x_0 - not on any "past history" of *x*.

At the optimal values of x_t , c_t , l_t we have

$$V(x_0) = u(c_0, l_0) + \beta \sum_{t=0}^{\infty} \beta^t u(c_{t+1}, l_{t+1})$$

= $u(c_0, l_0) + \beta V(x_1)$
= $u(c_0, l_0) + \beta V(x_0 + f(x_0, l_0) - c_0)$.

We can use this formula to find V for many different values of x_0 simultaneously.

Master-Worker An MW Example: Value Function Iteration

Bellman Equation for V(x)

We look for a function V that satisfies this relationship (for all x):

$$V(x) = \max_{(c,l)} u(c,l) + \beta V(x+f(x,l)-c).$$

This is the Bellman equation.

- The function V is unknown
- Parametric dynamic programming: Approximate V(x) by $\hat{V}(x; a)$, and solve for the parameters *a* using the Bellman equation.
 - simplest representation: $\hat{V}(x; a) = \sum_{j=1}^{p} a_j x^j$
 - find $a \in \mathbb{R}^{p+1}$ such that $\hat{V}(x; a)$ "approximately" satisfies the Bellman equation, on a finite grid of x values: x^1, x^2, \ldots, x^n . (Data Fitting.)

Master-Worker An MW Example: Value Function Iteration

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Value Function Iteration

- Step 0. *Initialization*. Choose functional form for $\hat{V}(x; a)$ and approximation grid $X = \{x_1, \dots, x_n\}$. Make initial guess $\hat{V}(x; a^0)$ and choose $\epsilon > 0$.
- Step 1. Maximization step. Fix $a^k = (a_j^k)_{j=1}^p$. For i = 1, ..., n, compute $v_i = T \hat{V}^k(x_i, a^k) = \max_{\substack{(c_i, l_i) \\ (c_i, l_i)}} u(c_i, l_i) + \beta \hat{V}(x_i + f(x_i, l_i) - c_i, a^k)$
- Step 2. Data Fitting for a: Fix c, I. Find a^{k+1} s.t. $a^{k+1} = \arg \min_{a} \|\hat{V}(x, a) - v\|^2$
- Step 3. Convergence. If $\|\hat{V}(x, a^{k+1}) \hat{V}(x, a^k)\|_{\infty} > \epsilon$, set $k \leftarrow k+1$ and go to Step 1; otherwise stop and report solution.

Master-Worker An MW Example: Value Function Iteration

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Value Function Iteration in MW

- MASTER: Initialization. Choose functional form for $\hat{V}(x; a)$ and approximation grid $X = \{x_1, \dots, x_n\}$. Make initial guess $\hat{V}(x; a^0)$ and choose $\epsilon > 0$.
- **JORKER:** Maximization: Fix $a^k = (a_j^k)_{j=1}^p$. For i = 1, ..., n, compute (in parallel) $v_i = T \hat{V}^k(x_i, a^k) = \max_{\substack{(c_i, l_i)}} u(c_i, l_i) + \beta \hat{V}(x_i + f(x_i, l_i) - c_i, a^k)$
- MASTER: Data Fitting: Fix c, I. Find a^{k+1} s.t. $a^{k+1} = \arg \min_{a} \|\hat{V}(x, a) - v\|^2$
- **MASTER:** Convergence. If $\|\hat{V}(x, a^{k+1}) \hat{V}(x, a^k)\|_{\infty} > \epsilon$, set $k \leftarrow k + 1$ and go to Step 1; otherwise stop.

Master-Worker An MW Example: Value Function Iteration

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MW Implementation

Each task finds the optimal (c_i, l_i) for a batch of x_i 's.

- Calls a simple FORTRAN code (to demonstrate that we can!) to do minimizations.
- Hot starting: the optimal (c_i, l_i) is usually a great starting point for (c_{i+1}, l_{i+1}) —so report these values to the master for use at the next iteration.
- The task wrapper (C++) and the FORTRAN code communicate via files.

Good algorithms are still vitally important!

A smart, hard-to-parallelize algorithm often beats a dumb, pleasantly parallel algorithm.

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act_on_complete_task() on the Master stores the v_i 's (and the c_i and l_i values) as they arrive from the workers. When all workers have reported, it solves the least-squares problem (fitting step) to find a^{k+1} .

- Could still take a fitting step without waiting for all tasks to report (partial information) to avoid hangups if some workers go down.
- Could adapt size of task (number of x_i's in each task) to accommodate workers of different speeds.

Master-Worker An MW Example: Value Function Iteration

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How Big Can These Get?

Judd: These models can get very big!!!

- Investment Portfolio
 - d assets in the portfolio
 - $X_j = \{x_{j1}, \ldots, x_{jn}\}$ represents *j*-th asset's position
 - state space: $X = X_1 \times X_2 \cdots \times X_d$
 - transaction cost occurs when adjusting asset positions
- Dynamic Principal-Agent Problem
 - the CEO's performance is evaluated by multiple measures, e.g. stock price, annual profits, etc.
 - the company decides the CEO's compensation package
- Many other economic applications

Master-Worker An MW Example: Value Function Iteration

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MWGAMS Running short-lived GAMS as a MW task

- MWGAMS is a MW application which runs GAMS in the worker
- Good for jobs with a lot of short optimization problems
- User writes entirely in GAMS no C++ code at all

The World of Condor

Summary

- Condor can easily manage dedicated and desktop machine
- Idle workstations can provide lots of compute cycles
- Master Worker is a good way to run massively parallel applications

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The World of Condor

Condor team



Greg Thain and Steve Wright Supercomputing with Condor

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The World of Condor

Condor in the US

pgflastimage

Greg Thain and Steve Wright Supercomputing with Condor

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The World of Condor

Condor in Europe

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Greg Thain and Steve Wright Supercomputing with Condor

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The World of Condor

Condor in the World

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Greg Thain and Steve Wright Supercomputing with Condor

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The World of Condor

For more information

- Talk to Greg or Steve!
 - gthain@cs.wisc.edu
- Condor web site: http://www.cs.wisc.edu
- Condor-users mailing list (see web site)
- Condor Week
- (If all else fails) 600 page condor manual
- Talk to Miron re: collaboration

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